## Computing the M Most Probable Modes of a Graphical Model – Supplemental Material

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This supplemental material contains detail of the experimental setup and additional results for the experiments on synthetic data and on the ChaLearn gesture recognition dataset.

## Synthetic Data

All synthetic experiments are performed using chain CRFs of length n = 100 with each variable taking one out of L = 8 states. We create ground truth labelings in the following way: for each ground truth instance, we create a  $L \times n$  matrix of uniformly random values, and we smooth it along the spatial dimension by convolving it with a Gaussian of standard deviation 7. Picking for each variable the state of highest value in the matrix, we obtain a labeling of the sequence with spatial correlation along the chain structure.

Training and test examples are creates as noisy instances of the ground truth: for each example, each variable is assigned an *L*-dimensional feature vectors that is the indicator vector of the corresponding state, distorted by zero-mean additive Gaussian noise of standard deviation  $\sigma$ . We train the CRF using the UGM package <sup>1</sup>. **Gesture Dataset** 

<sup>1</sup>http://www.di.ens.fr/~mschmidt/Software/UGM.html



Figure 1: An example data  $(L = 4, \sigma = 0.2)$ . Top: the true labeling.

Second to fifth row: perturbed features. The  $\ell$ -th feature is the indicator function of whether a node has label  $\ell$ , plus some noise.



Figure 2: Comparison of the three methods in synthetic experiment in terms of accuracy, top to down, left to right:  $\sigma = 0.5, 0.75, 1, \dots, 2.5$ .



Figure 3: Mode distribution. Top to down, left to right:  $\sigma = 0.5, 0.75, 1, \dots, 2.5$ .



Figure 4: Results on the gesture dataset: top to down, left to right: training set size is 10, 15, 20, 25 and 28 respectively. Top: accuracy, Bottom: modes distribution